



Cambridge International AS & A Level

CANDIDATE
NAME



CENTRE
NUMBER

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FURTHER MATHEMATICS

9231/33

Paper 3 Further Mechanics

May/June 2024

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use 10 ms^{-2} .

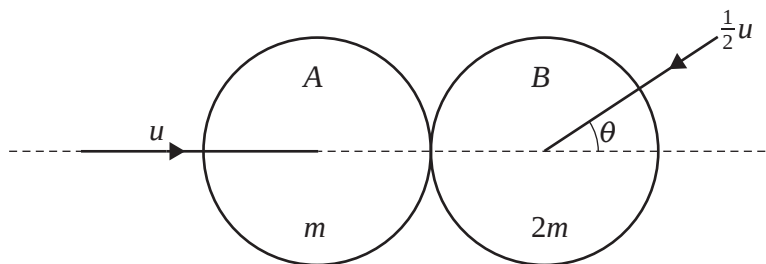
INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Any blank pages are indicated.



1



Two smooth uniform spheres A and B of equal radii have masses m and $2m$ respectively. The two spheres are moving on a smooth horizontal surface when they collide with speeds u and $\frac{1}{2}u$ respectively. Immediately before the collision, A 's direction of motion is along the line of centres, and B 's direction of motion makes an angle θ with the line of centres (see diagram).

As a result of the collision, the direction of motion of A is reversed and its speed is reduced to $\frac{1}{4}u$. The direction of motion of B again makes an angle θ with the line of centres, but on the opposite side of the line of centres. The speed of B is unchanged.

Find the value of the coefficient of restitution between the spheres.

[4]

[illegible]



- 3 A particle P of mass m is attached to one end of a light inextensible string of length a . The other end of the string is attached to a fixed point O . When the particle is hanging vertically below O , it is projected horizontally with speed u so that it begins to move along a circular path. When P is at the lowest point of its motion, the tension in the string is T . When OP makes an angle θ with the upward vertical, the tension in the string is S .

(a) Show that $S = T - 3mg(1 + \cos \theta)$. [5]

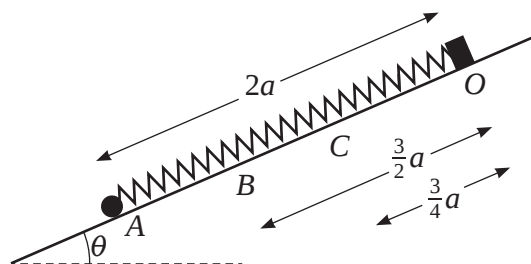
[illegible]



(b) Given that $u = \sqrt{4ag}$, find the value of $\cos \theta$ when the string goes slack.

[2]

This image shows a full page of a handwriting practice worksheet. It consists of multiple sets of three horizontal dashed lines, providing a guide for letter height and placement. The lines are evenly spaced across the entire page, leaving ample room for writing practice. There is no text or other markings on the page.



[7]

This image shows a full page of a handwriting practice worksheet. It consists of multiple rows of horizontal dashed lines spaced evenly apart, providing a guide for letter height and placement. The background is plain white, and there are no margins or additional markings.



7

[illegible]



The object ABC is suspended from C . In its equilibrium position, the side AB makes an angle θ with the vertical, where $\tan \theta = \frac{6}{5}$.

(b) Find x in terms of a .

[4]

This image shows a full page of a worksheet designed for handwriting practice. It consists of approximately 20 horizontal rows. Each row is defined by two parallel dotted lines, creating a series of uniform gaps where letters can be written. The lines are evenly spaced across the entire page, providing a guide for letter height and placement. There is no text or other markings on the page.



- 6** A particle P is projected with speed $u \text{ ms}^{-1}$ at an angle θ above the horizontal from a point O and moves freely under gravity. After 5 seconds the speed of P is $\frac{3}{4}u$.

(a) Show that $\frac{7}{16}u^2 - 100u \sin \theta + 2500 = 0$. [3]

[illegible]



(b) It is given that the velocity of P after 5 seconds is perpendicular to the initial velocity.

Find, in either order, the value of u and the value of $\sin \theta$. [5]

[illegible]



(b) Find an expression for x in terms of t .

[3]

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(c) Find the distance that the parachutist has fallen, since opening his parachute, when his speed is 15 m s^{-1} .

[2]

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Additional page

If you use the following page to complete the answer to any question, the question number must be clearly shown.

[illegible]

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15



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16

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